



Michigan Tech

# **COMSOL Multiphysics® Based Inductance Estimation for Modeling Transformer Winding Faults in EMTP**

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**COMSOL**  
**CONFERENCE**  
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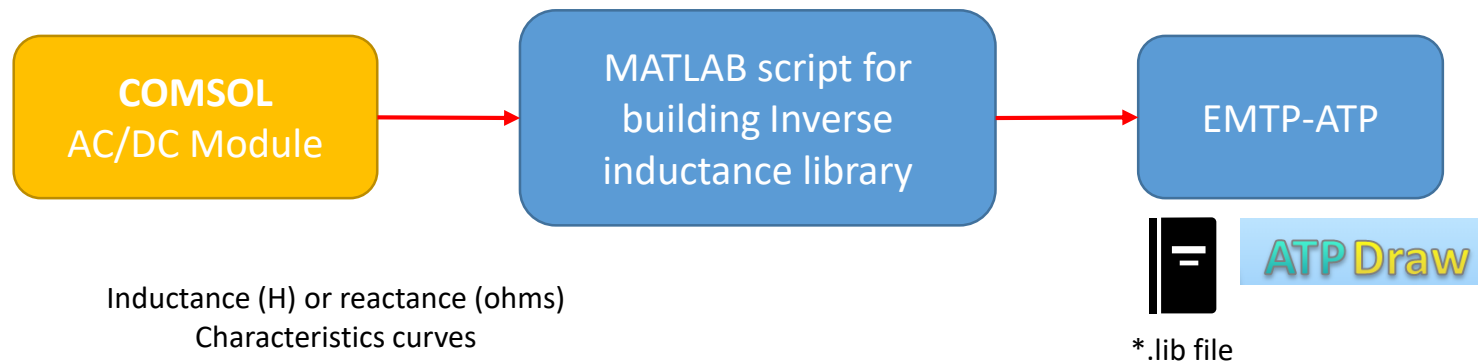


# INTRODUCTION:

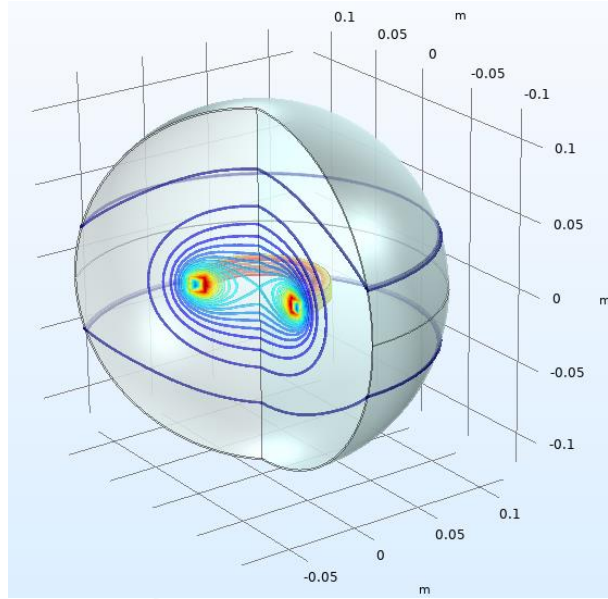
- ❑ Power Transformer are the most crucial element in power system network
- ❑ Protective systems are available to address the abnormality
  - Avoid relay mis-operation
  - Maintain reliability
- ❑ Inner winding faults produce minor current and are difficult to detect
  - Turn-to-turn winding fault (**T2T**)
  - Turn-to-ground winding fault (**T2G**)
- ❑ Transformer model is the key to study and analyze the behavior

## OBJECTIVE:

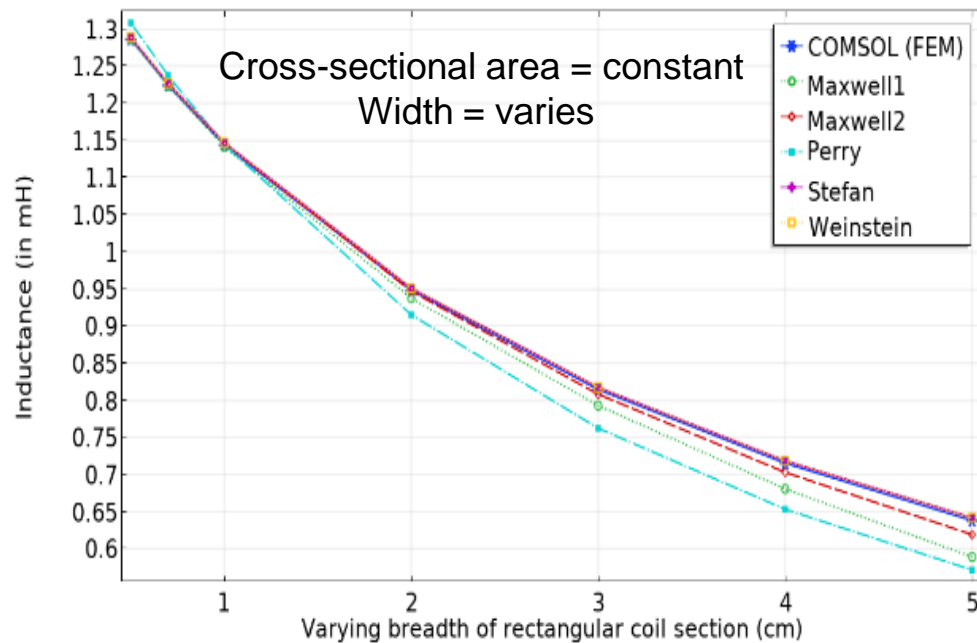
- ❑ Accurate representation of Transformer Winding fault
- ❑ Able to account minor effects
- ❑ Overcome simplification from Analytical Approaches
- ❑ Maintain user-friendly version of model for study and analysis
- ❑ EMTP-ATP Implementation worthy



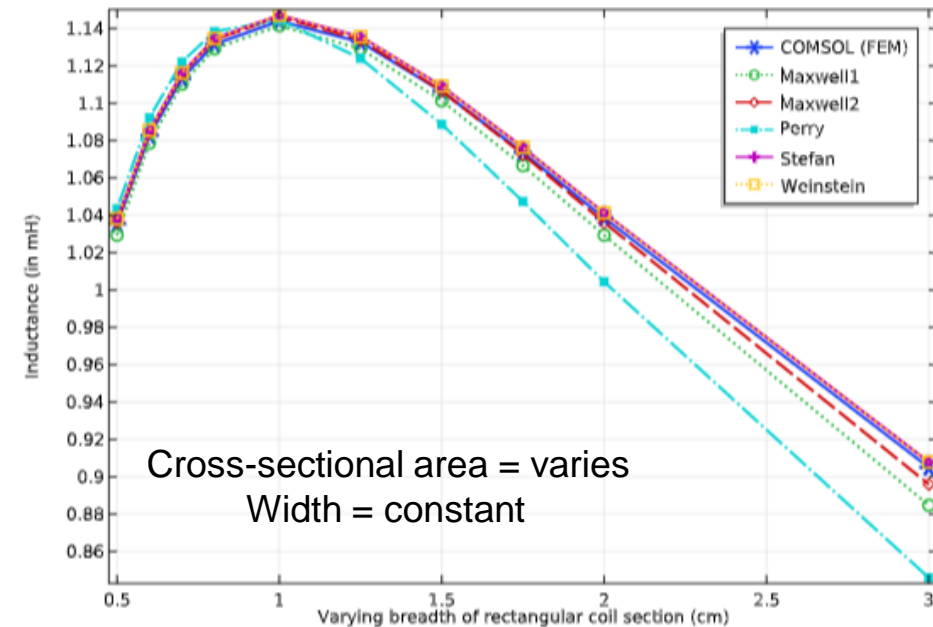
# Significance of FEA based approach



**Comparison of analytical approaches to estimate the inductance vs FEA method**

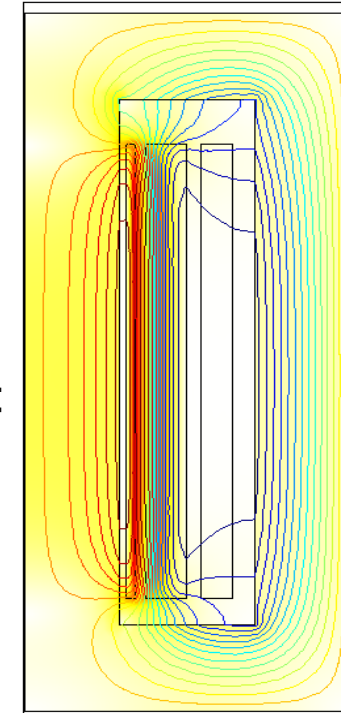
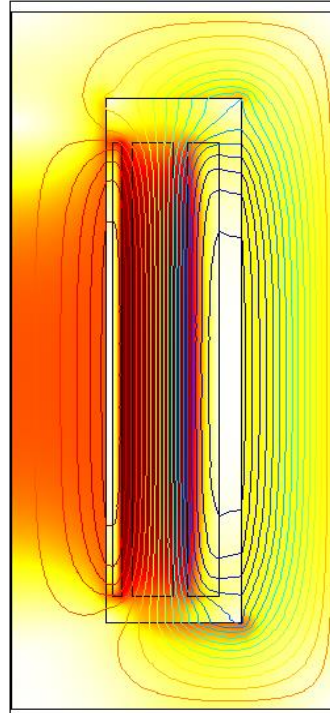
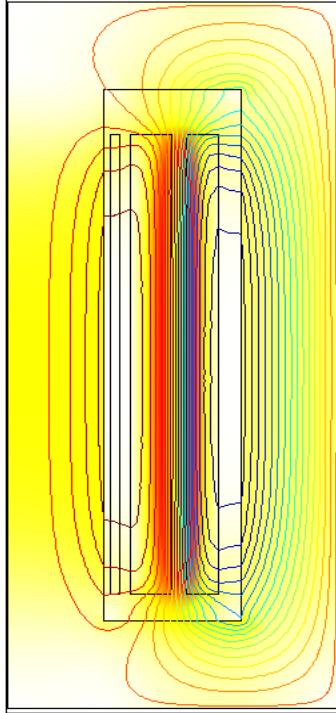


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# Method to estimate leakage inductances:

## Case A: Healthy Transformer



Leakage Reactance	Analytical formula based	COMSOL (FEA)
$X_{sc}$	21.2918	21.0572
$X_{sd}$	38.5627	38.1231
$X_{cd}$	11.7180	11.0950

# Inductance calculation from simulation

## Self and Mutual Inductance values

$$L_{12} = L_{\text{self1}} - \frac{M_{12}^2}{L_{\text{self2}}}$$

- One coil-pair at a time
- Coil 1 (source) = Current excitation (rated)
- Coil 2 (shorted) = Voltage excitation of 0V



Mf.L\_1\_3 (H) [mutual inductances b/w 1 & 3 ]

mf.LCoil\_3 (H) [Coil inductances]

## Magnetic Solution Method

$$L_{12} = \frac{2 * W_m}{I^2} = \frac{2 * \text{mf.int}W_m}{\text{mf.ICoil}_1^2}$$

- One coil-pair at a time
- Coil 1 = Current excitation (I1)
- Coil 2 = Current excitation (I2)
- I1 x N1 = I2 x N2 (AT balance)



mf.Wm (J) [Magnetic Energy Density]

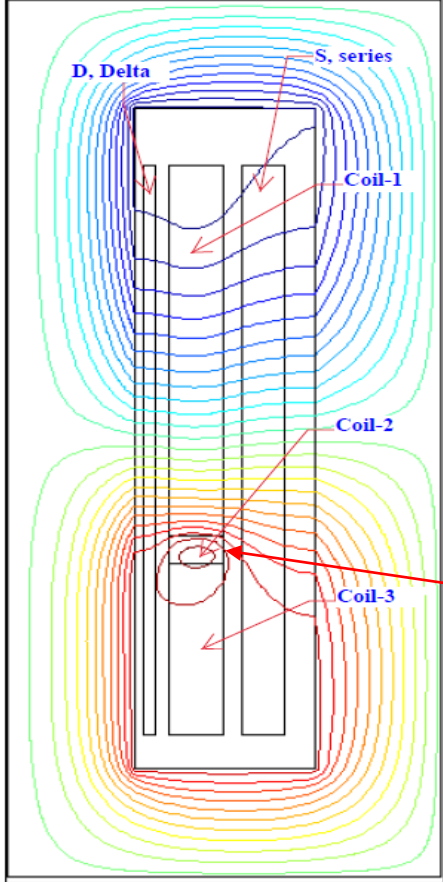
(user defined regions only)

or

mf.intWm (J) [Total Magnetic energy]

(covers all regions)

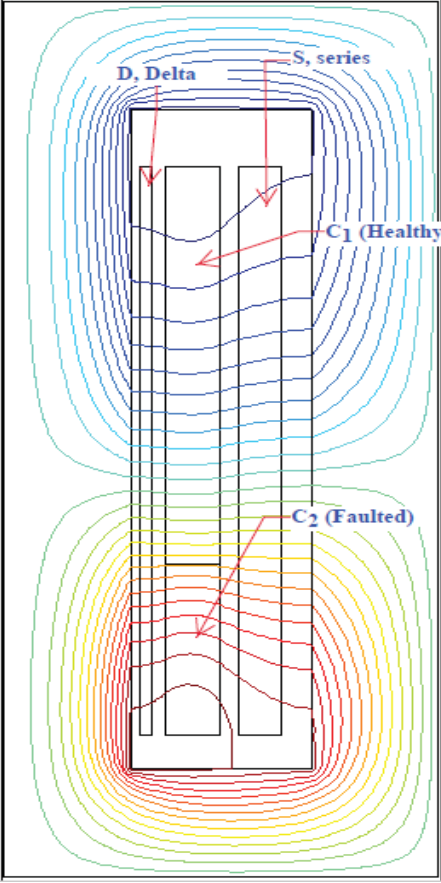
# Winding Fault simulations



T2T

Conceptual overview of T2T and T2G fault modeling on common winding

3 coil segments with coil 2 indicating faulted turns



T2G

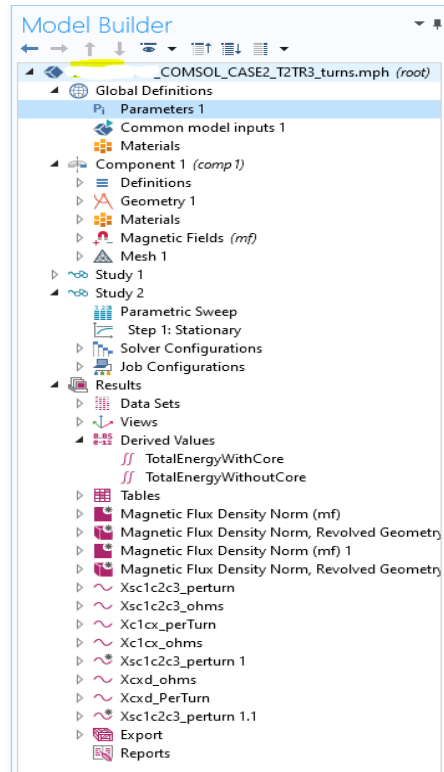
Challenge: To model for any range of fault progression



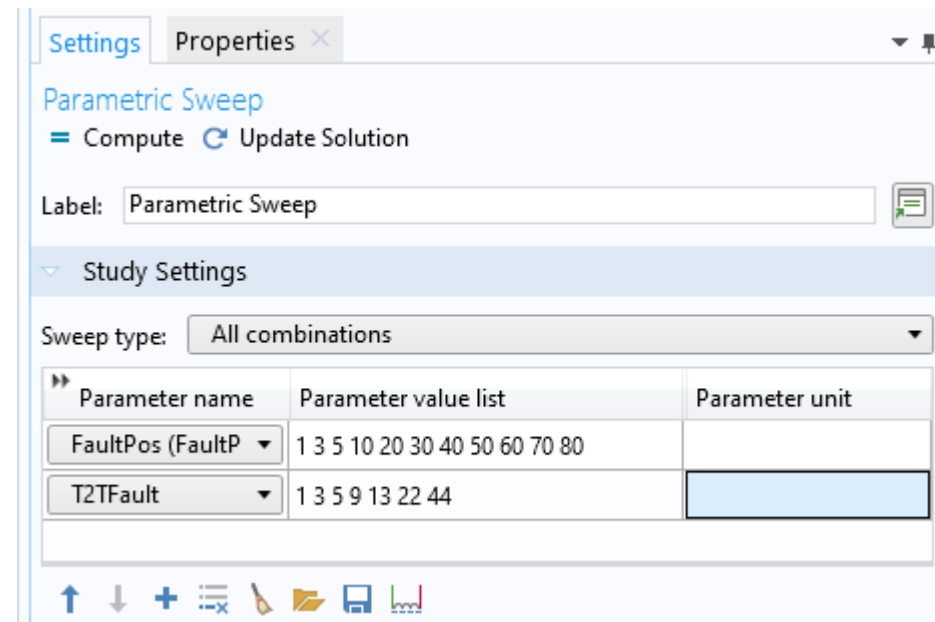
# Derive Characteristic curves

## Parametric Sweep approach:

- Magnetic solution method
- T2T or T2G
- Fault position progression from bottom to top
- Faster output
- Ability to post-process multiple simulation cases into a table

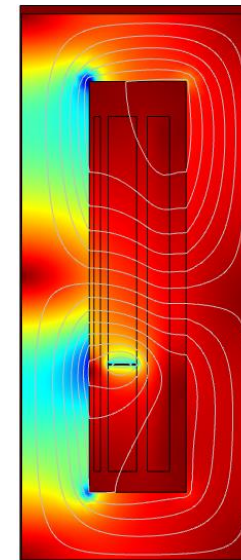
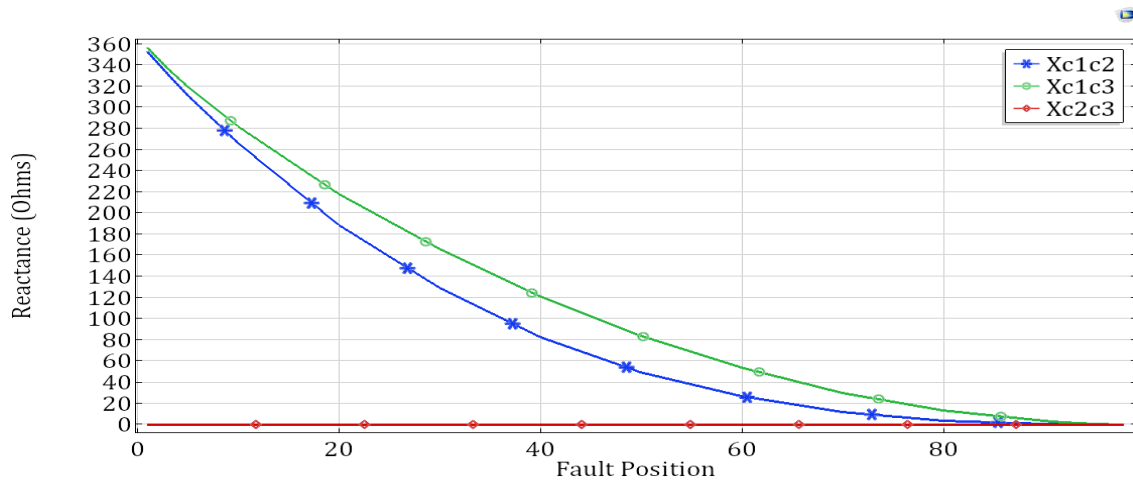
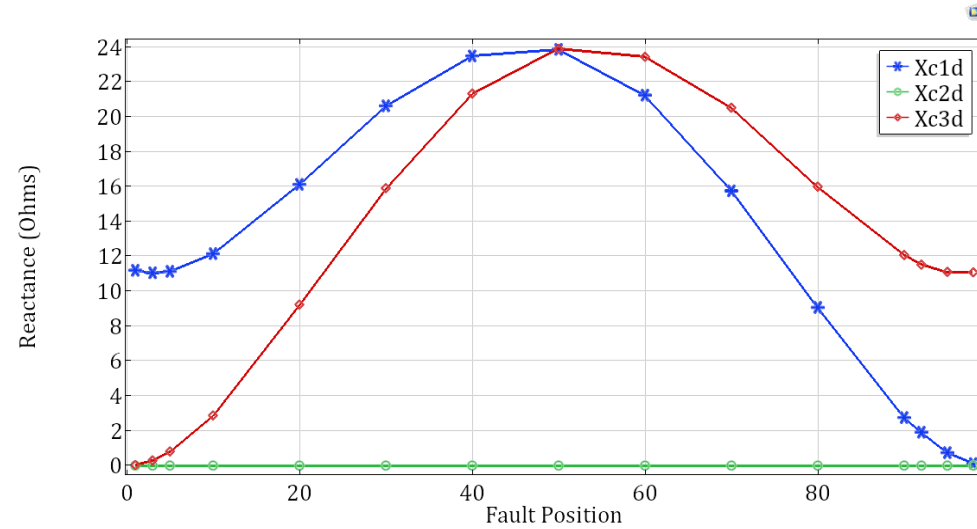
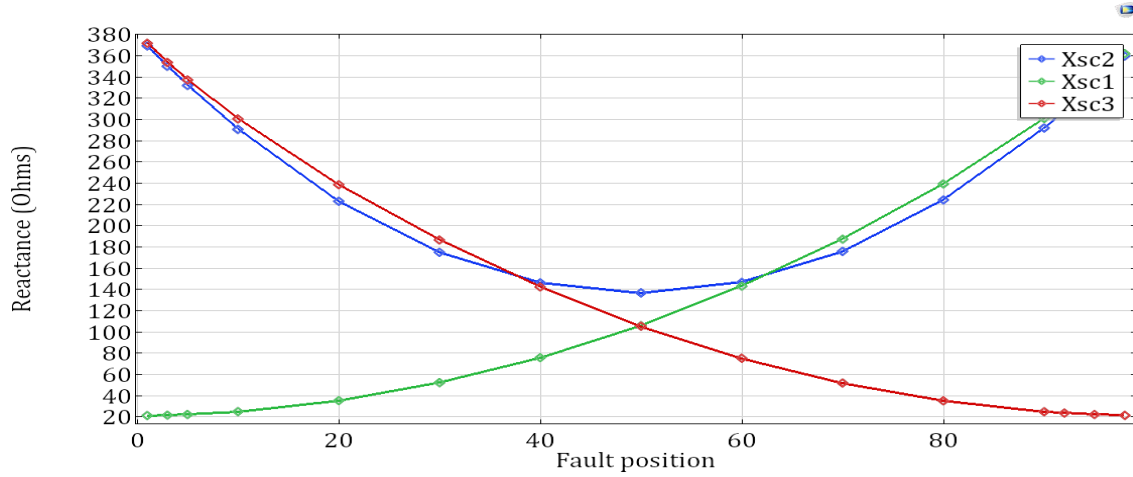


Name	Expression	Value	Description
C_height	1.496[m]	1.496 m	Common winding coil h...
FaultPos	30	30	FaultPosition
T2TFault	1	1	
C3_height	(FaultPos/100)*C_heig...	0.4488 m	
C2_height	(T2TFault/444)*C_height	0.0033694 m	
C1_height	C_height-C2_height-C...	1.0438 m	
Ns	444	444	
Nc	444	444	
Nd	140	140	
Nc1	Nc-Nc2-Nc3	310	
Nc2	T2TFault	1	
Nc3	round((FaultPos/100)*...	133	
Itest	-100[A]	-100 A	
Ic1	-kc1*Itest*Ntest/Nc1	0 A	
Ic2	-kc2*Itest*Ntest/Nc2	0 A	
Ic3	-kc3*Itest*Ntest/Nc3	0.75188 A	
kc1	0	0	
kc2	0	0	
kc3	1	1	
Ntest	Nc2	1	
Is	0	0	
Id	0	0	





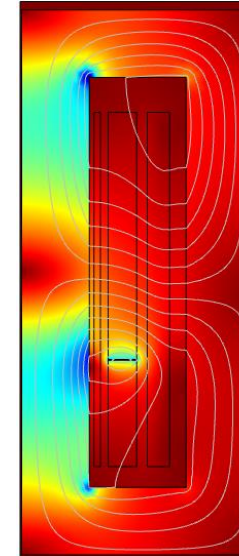
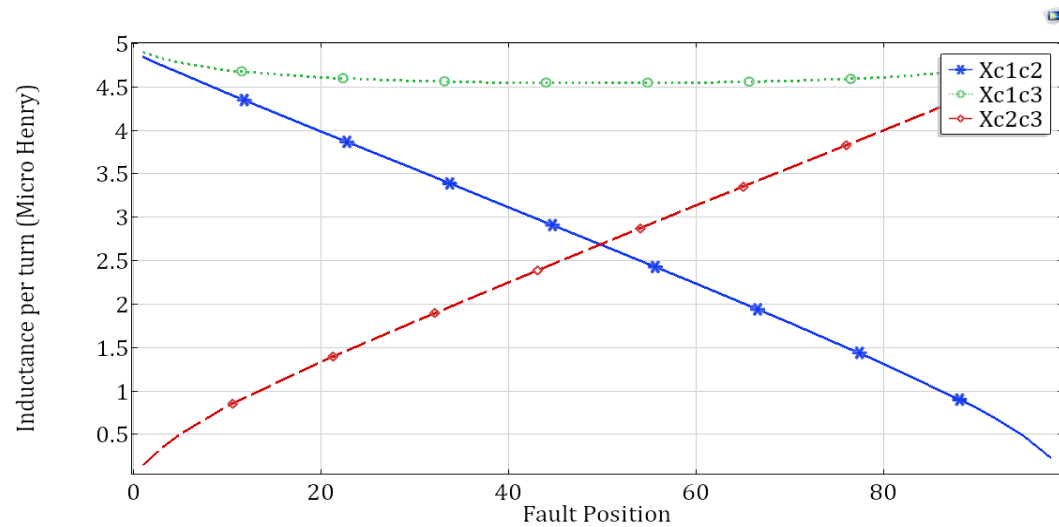
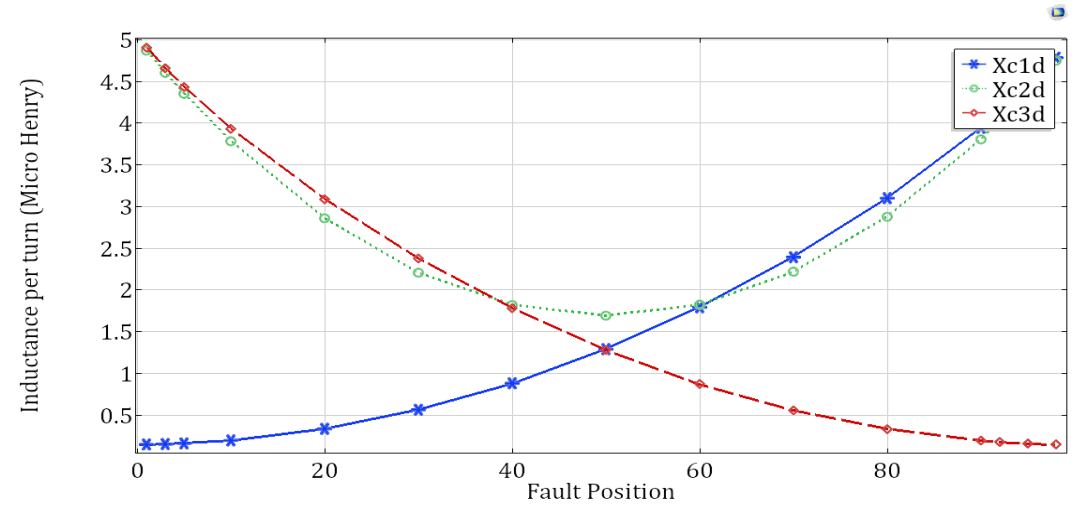
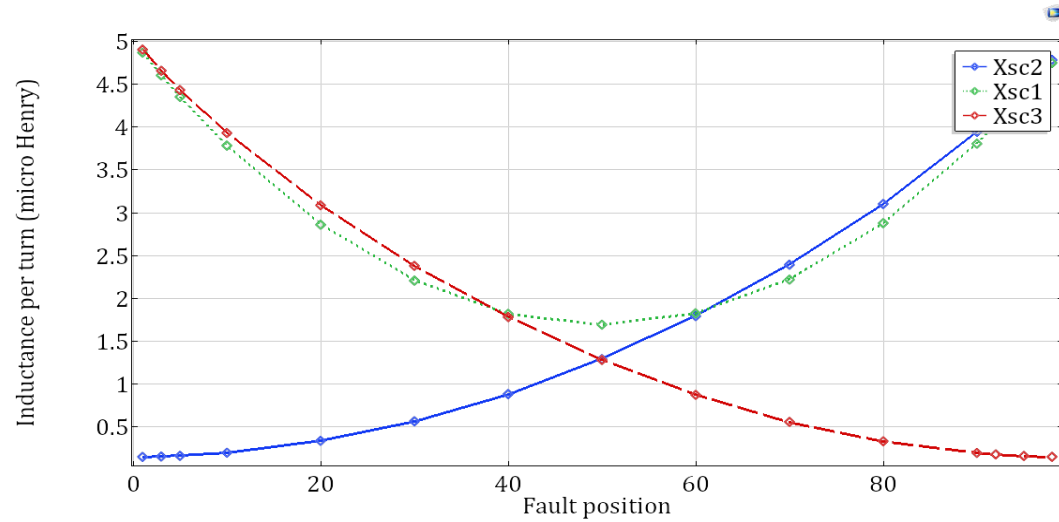
# Leakage reactance between coil segments: S, C1, C2, C3 and D



T2T fault on Common winding

- Reactance profile does not provide trend to simplify the curves

# Leakage inductances (1-turn basis) between coil segments: S, C1, C2, C3 and D



T2T fault on Common winding

- These curve are reduced to set of equation by fitting and supplied ad input to MATLAB codes

## Simulation Result in ATP:

	Expected [A]	Simulation [A]
Primary (A-ph)	3717.7	3710.29
Secondary (A-ph)	237.0	240.65
Tertiary (A-ph)	3121.6	3001.9
Primary (B-ph)	247.5	251.00
Secondary (B-ph)	644.6	644.22
Tertiary (B-ph)	3121.6	3001.8

## Conclusion:

- Accurately estimated the values of leakage reactance for healthy and faulted winding transformer
- Characteristic curve is exported or simplified by fitting the values
- The coefficients are then supplied to developed matlab code to generate library for near-real time
- Enhanced the ATP model for studying the Transformer protection

# References

1. Rosa, Edward B, Grover, Frederick W, and United States. “Formulas and Tables for the Calculation of Mutual and Self-Inductance”. U.S. Dept. of Commerce and Labor, *Bureau of Standards: U.S. Govt. Print. Off. 1912*. Web.
2. F. W. Grover, “Additions to the formulas for the calculation of mutual and self-inductance”. *U.S. Dept. of Commerce, Bureau of Standards: –U.S. Govt. Print. Off. 1919*.
3. Høidalen, Hans & A Mork, Bruce & Gonzalez-Molina, Francisco & Ishchenko, Dmitry & Chiesa, Nicola. (2009). Implementation and verification of the Hybrid Transformer model in ATPDraw. *Electric Power Systems Research*. 79. 454-459. 10.1016/j.epsr.2008.09.003.
4. Kulkarni, S. V., and Khaparde, S. A., “Transformer Engineering Design and Practice”. New York: Marcel Dekker, Inc., 2004. Print.
5. Blume, Louis Frederick et al., “Transformer Engineering; a Treatise on the Theory, Operation, and Application of Transformers”. New York: Wiley, 1938. Print.
6. E. O. Egorova, Development of the Coil Volume method for time-domain simulation of internal faults in transformers. PhD thesis, Michigan Technological University, Houghton, MI, USA, 2019.
7. **H. K. Vemprala, “Advancements in time-domain modeling for power system disturbances,” Ph.D. dissertation, Michigan Technological University, Houghton, MI, USA, 2019 (In progress).**
8. Walter Frei, “Exploiting Symmetry to Simplify Magnetic Field Modeling”, COMSOL Blog, July 14, 2014, web:<https://www.comsol.com/blogs/exploiting-symmetry-simplify-magnetic-field-modeling/>

